



Toward the correctness of TweetNaCl's Ed25519 with VST

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A quick overview of TweetNaCl



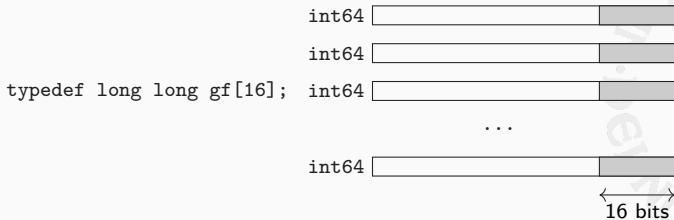
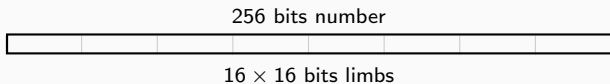
```

for(i=254;i>=0;--i) {
  r=(z[i>>3]>>(i&7))&1;
  sel25519(a,b,r);
  sel25519(c,d,r);
  A(e,a,c);           #
  Z(a,a,c);           #
  A(c,b,d);           # Montgomery Ladder
  Z(b,b,d);           #
  S(d,e);             # The steps and order
  S(f,a);             # of the operations
  M(a,c,a);           # have been proved
  M(c,b,e);           # by Timmy Weerwag
  A(e,a,c);           #
  Z(a,a,c);           #
  S(b,a);             # The use of datatypes
  Z(c,d,f);           # (number representation)
  M(a,c,_121665);    # is not proven (yet).
  A(a,a,d);           #
  M(c,c,a);           #
  M(a,d,f);           #
  M(d,b,x);           #
  S(b,e);             #
  sel25519(a,b,r);
  sel25519(c,d,r);
}

```

Code 1: crypto_scalarmult

256 bits integers does not fit into a 64 bits containers...



```
#define FOR(i,n) for (i = 0;i < n;++i)
#define sv static void
typedef long long i64;
typedef i64 gf[16];

sv A(gf o,const gf a,const gf b)    # Addition
{
    int i;
    FOR(i,16) o[i]=a[i]+b[i];      # carrying is done separately
}

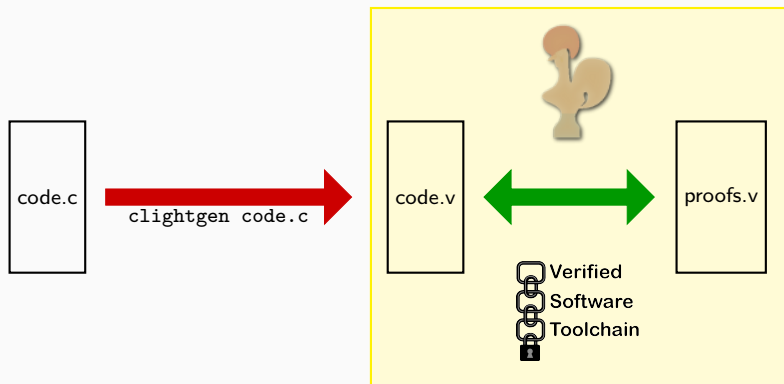
sv Z(gf o,const gf a,const gf b)    # Substraction
{
    int i;
    FOR(i,16) o[i]=a[i]-b[i];      # carrying is done separately
}

sv M(gf o,const gf a,const gf b)    # Multiplication
{
    i64 i,j,t[31];
    FOR(i,31) t[i]=0;
    FOR(i,16) FOR(j,16) t[i+j] = a[i]*b[j];
    FOR(i,15) t[i]+=38*t[i+16];
    FOR(i,16) o[i]=t[i];
    car25519(o);                   # carrying
    car25519(o);                   # carrying
}
```

Code 2: Basic Operations

From C to Coq





<http://vst.cs.princeton.edu>

<http://compcert.inria.fr>

```
Variable n: ℤ.  
Hypothesis Hn: n > 0.  
  
(*  
  in C we have gf[16] here we consider a list of integers (list ℤ)  
  of length 16 in this case.  
  
  ZofList convert a list ℤ into it's ℤ value  
  assume a radix: 2^n  
*)  
Fixpoint ZofList (a : list ℤ) : ℤ := match a with  
| [] ⇒ 0  
| h :: q ⇒ h + 2^n * ZofList q  
end.  
  
Notation "ℤ.lst A" := (ZofList A) (at level 65).
```

Code 3: ZofList


```
Fixpoint ZsumList (a b : list  $\mathbb{Z}$ ) : list  $\mathbb{Z}$  := match a,b with
| [], q  $\Rightarrow$  q
| q, []  $\Rightarrow$  q
| h1::q1,h2::q2  $\Rightarrow$  (Z.add h1 h2) :: ZsumList q1 q2
end.
```

Notation "A \boxplus B" := (ZsumList A B) (at level 60).

Corollary ZsumList_correct:

```
 $\forall$  (a b: list  $\mathbb{Z}$ ),
  (Z.lst a  $\boxplus$  b) = (Z.lst a) + (Z.lst b).
```

Qed.

Lemma ZsumList_bound_len:

```
 $\forall$  (m1 n1 m2 n2:  $\mathbb{Z}$ ) (a b: list  $\mathbb{Z}$ ),
  length a = length b  $\rightarrow$ 
  Forall ( $\lambda$  x  $\Rightarrow$  m1 < x < n1) a  $\rightarrow$ 
  Forall ( $\lambda$  x  $\Rightarrow$  m2 < x < n2) b  $\rightarrow$ 
  Forall ( $\lambda$  x  $\Rightarrow$  m1 + m2 < x < n1 + n2) (a  $\boxplus$  b).
```

Qed.

Code 4: Addition

What's left ?



- ▶ Specification of basic operations (A,Z,M,S,Car25519).
 - ▶ Bounds of basic operations.
 - ▶ Proof that model matches the semantic (code.v) using VST 🏆.
-
- ▶ ~10 months.
 - ▶ compiles (coqc) in ~1 hours . . . (i7-4770K CPU @ 3.50GHz)
 - ▶ 62 lines of C have been verified.
 - ▶ 7 180 lines of Specifications with Coq.
 - ▶ 2 872 lines of Verification with Coq using VST 🏆.



- ▶ Proof of a lot of *small* utilary functions used in TweetNaCl...
- ▶ Full Proof of Montgomery Ladder's correctness.
- ▶ Proof that the model is *aligned* with Timmy's work.
- ▶ Continue on the X25519 signature scheme, Poly1305...



Thank you.

